Solution on the three transformation method gave the following results (Table).
Transformation coefficients and estimate of accuracy are calculated by three methods

| Method | The solution by stretching method | The decision on the regression model with two-dimensional response on the basis of the generalized least-squares method | The decision on the regression model with two-dimensional response on the basis of the theorem about the characteristics of a multivariable conditional distribution law |
| :---: | :---: | :---: | :---: |
| Results of the solution | $\hat{x}=\left[\begin{array}{c}1.039159 \\ -0.816950 \\ 0.599934 \\ 1.258032 \\ 100.113 \\ 200.026\end{array}\right]$ | $\hat{k}=\left[\begin{array}{cc}1.039159 & 0.599934 \\ -0.816950 & 1.258032 \\ 100.113 & 200.026\end{array}\right]$ | $\begin{aligned} & \hat{X}=\left[\begin{array}{cc} 1.039159 & -0.816950 \\ 0.599934 & 1.258032 \end{array}\right] \\ & \hat{D}=\left[\begin{array}{l} 100.113 \\ 200.026 \end{array}\right] \end{aligned}$ |
| Estimate of accuracy | $\begin{aligned} & \hat{\sigma}_{o}=0.07824 \\ & \hat{\sigma}_{a}=\hat{\sigma}_{d}=0.000000938 \\ & \hat{\sigma}_{b}=\hat{\sigma}_{e}=0.000000661 \\ & \hat{\sigma}_{c}=\hat{\sigma}_{f}=0.00161753 \end{aligned}$ | $\begin{aligned} & \hat{\sigma}_{o}=0.07824 \\ & \hat{\sigma}_{a}=\hat{\sigma}_{d}=0.000000938 \\ & \hat{\sigma}_{b}=\hat{\sigma}_{e}=0.000000661 \\ & \hat{\sigma}_{c}=\hat{\sigma}_{f}=0.00161753 \end{aligned}$ | $\hat{\sigma}_{o}=0.07824$ |

Thus, the results of the calculation have shown that all three methods have presented similar conversion coefficients and the same estimate of accuracy. However, the second and third methods of transformation have a simpler realization of the algorithm. They were derived from the interpretation of the problem of transformation as a two-dimensional regression with two-dimensional response. Also the sense of the produced actions is visible at every step in the second and third approaches in contrast to the first transformation method. It allows better built calculations and analysis. Also it is important that the reducibility of a plane affine transformation to the two-dimensional regression with two-dimensional response makes it possible to use all the possibilities that are inherent of regression analysis, for example, determination, robustness, orthogonal regression, race-extension analysis. In its turn it makes it possible to obtain more qualitative and more adequate results of processing.

## REFERENCES

1. Дегтярев, А.М. Идентификация модели трансформации в геодезии на основе аффинного преобразования / А.М. Дегтярев, В.В. Ялтыхов // Автоматизированные технологии изысканий и проектирования. - 2013. № 2(49). - С. 71-74.
2. Ghilani, Charles D. Adjustment computations: spatial data analysis / Charles D. Ghilani, Paul R. Wolf. - Hoboken : JOHN WILEY \& SONS, INC., 2006. - 632 c.
3. Zellner, A. An Efficient Method of Estimating Seemingly Unrelated Regressions and Tests for Aggregation Bias / A. Zellner // Journal of the American Statistical Association. - Vol. 57, No. 298 (Jun., 1962). - C. 348-368.
4. Демиденко, Е.3. Линейная и нелинейная регрессии / Е.3. Демиденко. - М. : Финансы и статистика, 1981. 302 с.
5. Себер, Дж. Линейный регрессионный анализ / Дж. Себер, В.П. Носко ; под ред. М.Б. Малютова. - М. : Мир, 1980. - 456 с.
6. Андерсон, Т. Введение в многомерный статистический анализ / Т. Андерсон. - М. : Физматлит, 1963. - 500 с.

## UDC 528.5

# INVESTIGATION OF FEATURES SIGHT AND MEASUREMENT LINES USING GEODETIC REFLECTORS 

## KIRUL MARKOVICH <br> Polotsk State University, Belarus

The article presents an analysis of the errors of sight and measuring lines. These errors occur when nonstrict orientation geodetic reflector rangefinder. The dependence of the magnitude of the error on the conditions of orientation and design of the reflector.

Surveying reflectors are important devices in the production of surveying. However, many surveyors still pay attention to the characteristics of the tacheometer, forgetting about the impact on the accuracy of the
reflector. To perform high-precision measurements it is necessary to consider various factors of influence of geodetic reflectors on measurement of corners and distances.

The main factors that have the greatest impact on the results of geodetic measurements are precision centering of the reflector in the assembly (alignment of the reflector) and the strict orientation of the reflective surface on the rangefinder [1]. This article presents a study of the effect that occur when no strict orientation membrane and prismatic reflectors on the rangefinder.The study was performed at different times for the two lines of different lengths. The temperature and pressure were taken into account when measuring (table 1).

Table 1 - Characteristics of the measurement series

| Series | Measurement distance, <br> m | Temperature, $\mathrm{C}^{\circ}$ |  | Pressure, <br> Millimeter of mercury |
| :---: | :---: | :---: | :---: | :---: |
|  |  | end <br> of series |  |  |
| 1 | 50 | 9 | 6 | 749 |
| 2 | 100 | 15 | 13 | 747 |

The measurement was carried out on the lines in the membrane, and prismatic reflectors. Tacheometer Trimble M3 2013 DR5 " was used for the measurements. Accuracy of measurement lines Trimble M3 Total Station 2013 DR5 $2 \mathrm{~mm}+2 \mathrm{ppm}$ using a prism and $3 \mathrm{~mm}+2 \mathrm{ppm}$ in reflectorless mode. [2]

As the target points used prismatic reflector Leica Geosystems series GPH1 with precision centering of 2 mm [3], as well as the reflective film ORAFOL $100 \times 100 \mathrm{~mm}$ (fig. 1) [4].


Fig. 1. Construction of target points
The technique of research consisted in performance of measurements of lines and directions at a turn of reflectors with the set step in $10^{\circ}$ in horizontal (prismatic and membrane reflectors), vertical (prismatic) and the horizontal-vertical planes (prismatic). In all series measurement of distances on a prismatic reflector was carried out in the standard mode of a range finder of STD, measurement on a film reflector - in the reflectorless mode DR. The results were averaged over the three measured values. The study was performed in the conventional coordinate system. In the conventional system, the X -axis coincides with the line of sight to the reflector at the location of the reflective surface perpendicular (angle of rotation of the reflector is equal to 0 ).

The results of measurements of distances and directions are listed below. The data were obtained by averaging the values of three measurements. Tables $2,3,4$ presented experimental data for the distances of 50 and 100 meters. The turn of a prism is executed in the horizontal plane.

According to the results of the experiment with a prism pattern are the following:

1. The maximum reversal prism Leica GPH1 from the normal to the line of sight of $50^{\circ}$ in the horizontal plane at a distance of 50 meters and decreases with increasing length of the measured line;
2. The operating range of turning the prism increase the measured distance is not observed.
3. Turn the prism has a tendency:

- A significant angle of rotation in a horizontal plane for a distance of 50 and 100 meters making significant errors in the measurement of the horizontal direction and in the transverse component $\Delta \mathrm{Y}$.
- Turn in a vertical plane is significantly distorts the zenith distance and altitude component $\Delta \mathrm{Z}$.


## Technology, Machine-building, Geodesy

Table 2 - A prism turn in the horizontal plane ( $\mathrm{S} \approx 50,100 \mathrm{~m}$ )

| A prism turn in the horizontal plane |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| The angle of rotation | STD (prism, S $\sim 50 \mathrm{~m}$ ) |  |  |  |  | STD (prism, S $\sim 100 \mathrm{~m}$ ) |  |  |  |  |
|  | $\Delta \alpha$ | $\Delta \mathrm{z}$ | $\Delta \mathrm{X}, \mathrm{m}$ | $\Delta \mathrm{V}, \mathrm{m}$ | $\Delta \mathrm{Z}, \mathrm{m}$ | $\Delta \alpha$ | $\Delta \mathrm{z}$ | $\Delta \mathrm{X}, \mathrm{m}$ | $\Delta \mathrm{V}, \mathrm{m}$ | $\Delta \mathrm{Z}, \mathrm{m}$ |
| $50^{\circ}$ | -14' | 0 " | 0 | -0,004 | 0,001 | - | - | - | - | - |
| $40^{\circ}$ | -11" | -2" | 0 | -0,003 | 0,001 | -10" | -1" | -0,001 | -0,006 | 0 |
| $30^{\circ}$ | -6" | -1' | -0,001 | -0,001 | 0,001 | -8" | 2" | -0,003 | -0,004 | 0 |
| $20^{\circ}$ | -7" | -1" | -0,001 | -0,002 | 0,001 | -7" | -1" | -0,002 | -0,004 | 0,001 |
| $10^{\circ}$ | -5" | -2" | 0,001 | -0,001 | 0,001 | -4" | 2 " | -0,002 | -0,002 | -0,001 |
| $0^{\circ}$ | 0" | 90 ${ }^{\circ} 05^{\prime} 02^{\prime \prime}$ | 50,203 | 0,000 | 0,073 | 0' | 9004'47'' | 100,118 | $\mathbf{0 , 0 0 0}$ | 0,139 |
| $-10^{\circ}$ | 1 " | -1" | 0,002 | 0,001 | -0,001 | 2" | $1{ }^{\prime \prime}$ | -0,002 | 0,001 | 0 |
| $-20^{\circ}$ | 2" | $1{ }^{\prime \prime}$ | 0,001 | 0 | -0,001 | 5" | -1" | -0,002 | 0,002 | -0,001 |
| $-30^{\circ}$ | 3" | -1" | 0,001 | 0 | -0,001 | 7" | $1{ }^{\prime \prime}$ | 0,001 | 0,004 | 0 |
| $-40^{\circ}$ | 4" | 0 " | 0 | 0,001 | -0,001 | 10" | 2" | 0 | 0,007 | 0 |
| $-50^{\circ}$ | 8' | $0 "$ | 0,001 | 0,002 | -0,001 | - | - | - | - | - |




Fig. 2. The error of measurement directions and lines according to the angle of rotation of the prism in a horizontal plane

Table 3 - A prism turn in the vertical plane ( $\mathrm{S} \approx 50,100 \mathrm{~m}$ )

| A prism turn in the vertical plane |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| The angle of rotation | STD (prism, S $\sim 50 \mathrm{~m}$ ) |  |  |  |  | STD (prism, S $\approx 100 \mathrm{~m}$ ) |  |  |  |  |
|  | $\Delta \alpha$ | $\Delta \mathrm{z}$ | $\Delta \mathrm{X}, \mathrm{m}$ | $\Delta \mathrm{y}, \mathrm{m}$ | $\Delta \mathrm{Z}, \mathrm{m}$ | $\Delta \alpha$ | $\Delta \mathrm{z}$ | $\Delta \mathrm{X}, \mathrm{m}$ | $\Delta \mathrm{V}, \mathrm{m}$ | $\Delta \mathrm{Z}, \mathrm{m}$ |
| $40^{\circ}$ | -1" | -8" | -0,001 | 0 | 0,004 | 0" | -4" | 0,001 | 0.001 | 0,002 |
| $30^{\circ}$ | 0 " | -7" | 0 | 0 | 0,003 | -1" | -1" | 0.001 | 0 | 0.001 |
| $20^{\circ}$ | $0{ }^{\prime \prime}$ | -4" | -0,001 | 0 | 0,002 | 0" | -1" | -0,001 | 0 | 0,001 |
| $10^{\circ}$ | 0 " | -1" | -0,002 | 0 | 0 | -1" | -2" | 0 | 0 | 0.001 |
| $0^{\circ}$ | $0{ }^{\prime \prime}$ | 90 ${ }^{\circ} 05^{\prime} 02^{\prime \prime}$ | 50,203 | 0,000 | 0,073 | 0" | 90 ${ }^{\circ} 04{ }^{\prime} 47^{\prime \prime}$ | 100,118 | 0,000 | 0,139 |
| $-10^{\circ}$ | -2" | $5{ }^{\prime \prime}$ | 0 | -0,001 | -0,002 | $0{ }^{\prime \prime}$ | 3" | 0.001 | 0 | -0,001 |
| $-20^{\circ}$ | 1" | 7" | 0 | 0 | -0,003 | $0{ }^{\prime \prime}$ | 2" | -0.001 | 0 | -0,001 |
| $-30^{\circ}$ | 1" | 9" | 0 | 0 | -0,004 | $0{ }^{\prime \prime}$ | $5{ }^{\prime \prime}$ | 0 | 0 | -0,002 |
| -40 ${ }^{\circ}$ | 1" | 10" | 0 | 0 | -0,007 | 0' | 6 " | 0 | -0.001 | -0,003 |

(


Fig. 3. The error of measurement directions and lines according to the angle of rotation of the prism in a vertical plane

Table 4 - Turn the prism in horizontal and vertical planes ( $\mathrm{S} \approx 50$ and 100 m )

| Turn the prism in horizontal and vertical planes |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| The angle of rotation | STD (prism, S $\sim 50 \mathrm{~m}$ ) |  |  |  |  | STD (prism, S $\sim 100 \mathrm{~m}$ ) |  |  |  |  |
|  | $\Delta \alpha$ | $\Delta \mathrm{z}$ | $\Delta \mathrm{X}, \mathrm{m}$ | $\Delta \mathrm{V}, \mathrm{m}$ | $\Delta \mathrm{Z}, \mathrm{m}$ | $\Delta \alpha$ | $\Delta \mathrm{z}$ | $\Delta \mathrm{X}, \mathrm{m}$ | $\Delta \mathrm{V}, \mathrm{m}$ | $\Delta \mathrm{Z}, \mathrm{m}$ |
| $30^{\circ} / 30^{\circ}$ | -14" | -10" | 0 | -0,003 | 0.002 | -5" | -8" | 0 | -0,002 | 0.004 |
| $20^{\circ} / 20^{\circ}$ | -4" | -3" | -0,001 | -0,001 | 0,001 | -4" | -6" | -0,001 | -0,002 | 0,002 |
| $10^{\circ} / 10^{\circ}$ | -5" | -1" | -0,002 | -0,001 | 0 | -2" | -2" | -0,001 | -0,001 | 0,001 |
| $0^{\circ} /{ }^{\circ}$ | 0" | 9005'02' | 50,203 | 0,000 | 0,073 | $0{ }^{\prime \prime}$ | 9004'47'' | 100,118 | 0,000 | 0,132 |
| $-10^{\circ} /-10^{\circ}$ | 1' | 3" | 0 | 0 | -0,001 | 0 " | $1{ }^{\prime \prime}$ | -0,001 | 0 | 0 |
| $-20^{\circ}-20^{\circ}$ | 2" | 2" | 0 | 0,001 | -0,001 | 2" | 3" | -0,001 | 0,001 | -0,001 |
| -30\%-30 ${ }^{\circ}$ | $6{ }^{\prime \prime}$ | 5" | 0,001 | 0,002 | -0,002 | $6{ }^{\prime \prime}$ | 8' | -0,001 | 0,003 | -0,003 |



Fig. 4. The error of measurement directions and lines according to the angle of rotation of the prism in a horizontal and vertical plane

Table 2 - A membrane reflector turn in the horizontal plane ( $\mathrm{S} \approx 50,100 \mathrm{~m}$ )

| A membrane reflectors turn in the horizontal plane |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| The angle of rotation | DR (membrane reflector, $\mathrm{S} \approx 50 \mathrm{~m}$ ) |  |  |  |  | DR (membrane reflector, $\mathrm{S} \approx 100 \mathrm{~m}$ ) |  |  |  |  |
|  | $\Delta \alpha$ | $\Delta \mathrm{z}$ | $\Delta \mathrm{X}, \mathrm{m}$ | $\Delta \mathrm{y}, \mathrm{m}$ | $\Delta \mathrm{Z}, \mathrm{m}$ | $\Delta \alpha$ | $\Delta \mathrm{z}$ | $\Delta \mathrm{X}, \mathrm{m}$ | $\Delta \mathrm{y}, \mathrm{m}$ | $\Delta \mathrm{Z}, \mathrm{m}$ |
| $60^{\circ}$ | 10" | $1{ }^{\prime \prime}$ | 0,003 | 0,000 | 0 | 11" | $1{ }^{\prime \prime}$ | 0,002 | 0,000 | 0 |
| $50^{\circ}$ | $9{ }^{\prime \prime}$ | 0 " | 0,002 | 0,001 | -0,001 | 10" | 1 " | 0,002 | 0,001 | -0,001 |
| $40^{\circ}$ | 6 " | $0{ }^{\prime \prime}$ | 0,002 | 0,000 | 0 | 7" | 0 " | 0,002 | 0,000 | 0 |
| $30^{\circ}$ | 4" | 1 " | 0,002 | 0,001 | -0,001 | $6{ }^{\prime \prime}$ | 1" | 0,001 | -0,001 | 0 |
| $20^{\circ}$ | 3" | 1 " | 0,002 | 0,001 | 0 | 2" | --1" | 0 | 0 | 0 |
| $10^{\circ}$ | 1" | 0 " | 0,001 | 0 | 0 | 2" | 0 " | 0,001 | 0 | 0 |
| $0^{\circ}$ | $0{ }^{\prime \prime}$ | 8948'27'' | 50,364 | 0,000 | 0,169 | $0{ }^{\prime \prime}$ | 89 ${ }^{\circ} 54{ }^{\prime} 32^{\prime \prime}$ | 75,012 | 0,000 | 0,260 |
| $-10^{\circ}$ | -2" | 1 " | 0,001 | 0,000 | 0 | -1" | 0' | 0,001 | 0 | 0 |
| $-20^{\circ}$ | -3" | 1 " | 0 | 0,001 | 0,001 | -3" | -1" | 0 | -0,001 | 0 |
| $-30^{\circ}$ | -5" | 0 " | 0,001 | 0,000 | 0 | -5" | 0 " | 0,001 | 0,000 | 0 |
| -40 ${ }^{\circ}$ | -6' | 1 " | 0,002 | -0,001 | 0,001 | -7' | 1" | 0,001 | 0,000 | 0,001 |
| $-50^{\circ}$ | -8" | -1" | 0,002 | 0,000 | 0,001 | -8" | -1" | 0,002 | -0,001 | 0,001 |
| $-60^{\circ}$ | -11" | 0' | 0,003 | 0,000 | 0 | -9" | 0' | 0,001 | 0,000 | 0 |




Fig. 6. The error of measurement directions and lines
according to the angle of rotation of the membrane reflector in a vertical plane

Turn in both planes has a general tendency of errors for the transverse component and horizontal directions, and for vertical component and zenith distances.

The results of the experiment with membrane reflector contains the following laws:

1. The maximum reversal membrane reflector from the normal to the line of sight is $60^{\circ}$. Growth of the angle of rotation of the membrane reflector is accompanied by a linear tendency to increase the measured distance.
2. The maximum reversal membrane reflector from the normal to the line of sight does not introduce errors in the results of measurement of a horizontal direction and a transverse component of $\Delta \mathrm{U}$.

On the basis of the experiments the following conclusions:
1.The maximum range of the angles of rotation prism is $40^{\circ} \ldots 50^{\circ}$, which is slightly smaller than the membrane reflector $60^{\circ}$. This difference is due to the design of the prism body. The maximum rotation angle of the prism depends on the measured distance.
2. the measurements on film reflector, an increase of the measured distance with the increase of the angle of rotation of the reflector.
3. Work reversal prism in the horizontal and vertical planes is $20^{\circ}$. After turning $20^{\circ}$ in the measurement results include significant errors. Acceptable reversal film reflector, in which the measured distance changes slightly, $40^{\circ}-50^{\circ}$.
4. Turn the prism in the horizontal plane showed a tendency to increase measurement errors horizontal directions. Turn the prism in the vertical plane showed a tendency to increase measurement error zenith distances. Turn the membrane reflector in the horizontal plane does not introduce errors in the measurement of the horizontal direction.
5. Based on these results it can be argued that the use of the prism when performing high-precision engineering and surveying, as well as the use of film for fixing reflectors geodetic networks for works of high precision is possible only when the strict orientation of the reflecting surface in the rangefinder.

## REFERENCES

1. Спиридонов, Ю.В. Ошибки визирования при наблюдениях на призменные отражатели / Ю.В. Спиридонов // Credo-Dialogue. Проблемы и решения. - 2004. - № 13.
2. Электронный тахеометр Trimble серии M3 DR 2", $3^{\prime \prime}, 5^{\prime \prime}$. Руководство пользователя, 2009.
3. LEICA Surveying Reflectors -White Paper Characteristics and Influences [Electronic resource]. - Mode of access: https://www.yumpu.com/en/document/view/28954131/surveying-reflectors-white-paper-characteristics-and-influences. - Date of access: 03.05.2015.
4. ORAFOL [Electronic resource]. - Mode of access: http://www.orafol.com/corp/europe/ru /frontpage. - Date of access: 03.05.2015

## UDC 681.518.3:911.375.62

## APPLICATION OF GIS-TECHNOLOGIES FOR INFORMATION SUPPORT OF DECISION-MAKING MANAGEMENT AT THE LOCAL LEVEL

## MARYNA MAKARAVA <br> Polotsk State University, Belarus

The article presents an example of creation and possibility to use geographic information system for the management of urban areas. The structure and data organization in a municipal GIS are presented. The possibility of a comprehensive approach to municipal management with application of remote sensing ( $R S$ ) that allows providing government institutions, profit organizations and urban population with current information is reflected.

To meet the challenges of the UN programme "Goals of sustainable development" from 2015, that has underlined the importance of geospatial information, as well as in connection with the concept of informatization of the Republic of Belarus, work package for information and analytical support of all areas of national economy activities are planned to be carried out in the country.

To improve the management functions at the global and regional levels, it is necessary to start with changes in local territorial units. Geographic information systems are systems of collection, storage, analysis and graphical visualization of spatial data. ${ }^{[1]}$ Municipal service management is one of the largest application field of

